

**LESSON**  
**8-2**

# Graphing More Complicated Rational Functions

## Reteach

### Characteristics of Rational Functions

Vertical asymptotes	Zeros of denominator
Holes	Shared zeros of numerator and denominator
x-intercepts	Zeros of numerator
y-intercept	Value of function at $x = 0$ , $f(0)$

### Example

Find the vertical asymptote(s), hole(s), x-intercept(s), and y-intercept of:  $f(x) = \frac{x^2 + 2x - 15}{x^2 - x - 6}$

**Step 1** Write function in factored form.

$$\begin{aligned} f(x) &= \frac{x^2 + 2x - 15}{x^2 - x - 6} \\ &= \frac{(x + 5)(x - 3)}{(x - 3)(x + 2)} \end{aligned}$$

**Step 2** Find zeros of numerator and denominator.

Zeros of numerator:  $x = -5$ ;  $x = 3$   
Zeros of denominator:  $x = 3$ ;  $x = -2$

**Step 3** Find  $f(0)$ .

$$f(0) = \frac{0^2 + 2(0) - 15}{0^2 - 0 - 6} = \frac{5}{3}$$

Vertical Asymptote  
 $x = -2$

Hole  
 $x = 3$

x-intercept  
 $(-5, 0)$

y-intercept  
 $\left(0, \frac{5}{3}\right)$

**Find the vertical asymptote(s), holes, x-intercept(s), and y-intercept of the functions.**

1.  $f(x) = \frac{x + 6}{x^2 - 4x - 12}$

Vertical Asymptote(s): \_\_\_\_\_

Hole(s): \_\_\_\_\_

x-intercept(s): \_\_\_\_\_

y-intercept: \_\_\_\_\_

2.  $f(x) = \frac{x^2 + 7x + 12}{x^2 + 2x - 8}$

Vertical Asymptote(s): \_\_\_\_\_

Hole(s): \_\_\_\_\_

x-intercept(s): \_\_\_\_\_

y-intercept: \_\_\_\_\_

3.  $f(x) = \frac{x^2 - 1}{x - 4}$

Vertical Asymptote(s): \_\_\_\_\_

Hole(s): \_\_\_\_\_

x-intercept(s): \_\_\_\_\_

y-intercept: \_\_\_\_\_

4.  $f(x) = \frac{x + 2}{x^2 + 2}$

Vertical Asymptote(s): \_\_\_\_\_

Hole(s): \_\_\_\_\_

x-intercept(s): \_\_\_\_\_

y-intercept: \_\_\_\_\_