

# Multiplying and Dividing Rational Expressions

## Reteach

**Example** Find the product and any excluded values.

$$\frac{x^2 - 2x - 8}{x^2 - 1} \cdot \frac{x - 1}{x^2 - x - 6}$$

$$= \frac{(x - 4)(x + 2)(x - 1)}{(x + 1)(x - 1)(x - 3)(x + 2)}$$

$$= \frac{\cancel{(x - 4)}\cancel{(x + 2)}\cancel{(x - 1)}}{\cancel{(x + 1)}\cancel{(x - 1)}(x - 3)\cancel{(x + 2)}}$$

$$= \frac{x - 4}{(x + 1)(x - 3)}$$

**Step 1** Factor and multiply.

**Step 2** Cancel common factors.

**Step 3** Write simplified product.

**Step 4** Note excluded values.

$$x \neq -2, x \neq -1, x \neq 1, x \neq 3$$
**Find the product and any excluded values.**

$$1. \frac{x^2 - 5x - 14}{x^2 - 16} \cdot \frac{x^2 - x - 20}{x + 2} \quad 2. \frac{x^2 + 6x - 16}{x^2 - 3x} \cdot \frac{x}{x^2 - 3x + 2} \quad 3. \frac{x^2 - 14x + 45}{6x^2 - 3x} \cdot \frac{3x}{2x^2 - 50}$$


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**Example** Find the quotient and any excluded values.

$$\frac{x^2 - x - 12}{x + 5} \div \frac{x^2 + 9x + 18}{2x + 10}$$
**Step 1** Rewrite as multiplication by reciprocal of divisor.

$$= \frac{x^2 - x - 12}{x + 5} \cdot \frac{2x + 10}{x^2 + 9x + 18}$$

$$= \frac{(x - 4)(x + 3)}{x + 5} \cdot \frac{2(x + 5)}{(x + 6)(x + 3)}$$

$$= \frac{2(x - 4)(x + 3)(x + 5)}{(x + 5)(x + 6)(x + 3)}$$

$$= \frac{2(x - 4)\cancel{(x + 3)}\cancel{(x + 5)}}{\cancel{(x + 5)}(x + 6)\cancel{(x + 3)}}$$

$$= \frac{2(x - 4)}{(x + 6)}$$

**Step 2** Factor**Step 3** Multiply**Step 4** Cancel common factors.**Step 5** Write simplified product.**Step 6** Note excluded values.

$$x \neq -6, x \neq -5, x \neq -3$$

**Find the quotient and any excluded values.**

$$4. \frac{x^2 - 7x - 18}{2x^2 - 32} \div \frac{x^2 + x - 2}{2x - 8} \quad 5. \frac{3x^2 + 6x + 3}{x + 5} \div \frac{3x + 3}{x^2 - 25} \quad 6. \frac{2x^2 - 3x + 1}{5x^2} \div \frac{12x - 6}{10x^3 + 5x^2}$$


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